

The integral

$$\int e^{-x^2} dx$$

arises frequently in analyses of many mechanical, electrical, chemical, and biological processes. To 15 digits, the abscissas and weights for the 4–point and 5–point Gauss quadratures are

4–Point Gauss Quadrature	
t_k	w_k
–0.86113 63115 94053	0.34785 48451 37454
–0.33998 10435 84856	0.65214 51548 62546
0.33998 10435 84856	0.65214 51548 62546
0.86113 63115 94053	0.34785 48451 37454

5–Point Gauss Quadrature	
t_k	w_k
–0.90617 98459 38664	0.23692 68850 56189
–0.53846 93101 05683	0.47862 86704 99366
0.00000 00000 00000	0.56888 88888 88889
0.53846 93101 05683	0.47862 86704 99366
0.90617 98459 38664	0.23692 68850 56189

1. Approximate the integral

$$\int_{-1}^4 e^{-x^2} dx$$

using 4–point Gauss quadrature.

Answer: 1.6428 6173 7419.

2. Approximate the integral

$$\int_{-1}^4 e^{-x^2} dx$$

using 5–point Gauss quadrature.

Answer: 1.6485 3667 1769.

3. A 30–point Gauss quadrature will exactly integrate (without error) all polynomials up to what degree?
4. **True / False:** Gauss quadrature is used only to integrate polynomials.